

**Appendix S2.** Details of theoretical carbon balance simulations.**A. Details of leaf gas exchange and energy balance model**

We calculated “positive carbon balance” ( $C$ ) for each member of the four simulated populations, described in the next section, from a carbon balance, given by

$$C = A - \chi_w E - \chi_t H, \quad (\text{Eq. S1})$$

where  $A$  is leaf net  $\text{CO}_2$  assimilation rate ( $\mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1}$ ),  $E$  is leaf transpiration rate ( $\text{mol H}_2\text{O m}^{-2} \text{ s}^{-1}$ ),  $\chi_w$  is an assumed amortized cost of acquiring and transporting water from the soil to leaves to match the transpiration demand ( $\mu\text{mol CO}_2 \text{ mol}^{-1} \text{ H}_2\text{O}$ ),  $H$  is relative trichome density (unitless;  $H$  = whole-leaf trichome density divided by its population median), and  $\chi_t$  is the amortized carbon cost of constructing trichomes per unit of relative trichome density ( $\mu\text{mol C m}^{-2} \text{ s}^{-1}$ ). Estimation of  $\chi_w$  and  $\chi_t$  is described in section B, Parameter estimation below.

We calculated  $A$  from the Farquhar et al. (1980) biochemical model, which predicts  $A$  as the lesser of two values:  $A_v$  (limited by RuBP carboxylation rate) and  $A_j$  (limited by RuBP regeneration rate). In practice, we used hyperbolic minimization to smooth the transition between the two limitations:

$$A = \frac{0.5}{\theta_A} \left( A_v + A_j - \sqrt{(A_v + A_j)^2 - 4\theta_A A_v A_j} \right), \quad (\text{Eq. S2})$$

where  $\theta_A = 0.99$  is a dimensionless curvature parameter. We calculated  $A_v$  and  $A_j$  as

$$A_v = V_m \frac{c_i - \Gamma_*}{c_i + K_c \left( 1 + \frac{O}{K_o} \right)} - R_d \quad \text{and} \quad (\text{Eq. S3})$$

$$A_j = \frac{J}{4} \cdot \frac{c_i - \Gamma_*}{c_i + 2\Gamma_*} - R_d, \quad (\text{Eq. S4})$$

where  $V_m$  is the maximum velocity of RuBP carboxylation,  $c_i$  is intercellular CO<sub>2</sub> mole fraction ( $\mu\text{mol mol}^{-1}$ ),  $\Gamma^*$  is the photorespiratory CO<sub>2</sub> compensation point ( $\mu\text{mol mol}^{-1}$ ),  $K_c$  and  $K_o$  ( $\mu\text{mol mol}^{-1}$ ) are the Michaelis constants for RuBP carboxylation and oxygenation, respectively,  $O$  is the mole fraction of O<sub>2</sub> (210,000  $\mu\text{mol mol}^{-1}$ ),  $R_d$  is the rate of non-photorespiratory CO<sub>2</sub> release ( $\mu\text{mol m}^{-2} \text{s}^{-1}$ ), and  $J$  is the potential electron transport rate ( $\mu\text{mol m}^{-2} \text{s}^{-1}$ ). We calculated  $A_v$  and  $A_j$  using values of  $c_i$  calculated for each limitation by combining Eqs. **Error! Reference source not found.S3** or **Error! Reference source not found.S4**, respectively, with the diffusional constraint on CO<sub>2</sub> assimilation (Eq. **Error! Reference source not found.S5**) and solving the quadratic expression that results for  $c_i$ . The diffusional constraint is

$$A = g_{tc}(c_a - c_i), \quad (\text{Eq. S5})$$

where  $g_{tc}$  ( $\text{mol m}^{-2} \text{s}^{-1}$ ) is total conductance to CO<sub>2</sub> and  $c_a$  is ambient CO<sub>2</sub> mole fraction ( $\mu\text{mol mol}^{-1}$ ).  $g_{tc}$  is the sum of abaxial and adaxial values:

$$g_{tc} = g_{tc,ab} + g_{tc,ad}, \quad (\text{Eq. S6})$$

which in turn are parallel sums of stomatal and boundary layer conductances:

$$g_{tc,x} = (g_{sc,x}^{-1} + g_{bc,x}^{-1})^{-1}, \quad (\text{Eq. S7})$$

where  $x$  denotes abaxial or adaxial. We calculated  $g_{sc}$  for each surface from stomatal conductance to water vapor,  $g_{sw}$ , as  $g_{sc} = g_{sw}/1.6$ , reflecting the smaller diffusivity for CO<sub>2</sub> than for H<sub>2</sub>O, and we calculated  $g_{bc}$  from boundary layer conductance for water vapor as  $g_{bc} = g_{bw}/1.37$ , which reflects the partial contribution of advection (which is not affected by molecular diffusivity) to transport through the boundary layer.  $g_{sw}$  was determined from stomatal density for each surface separately as

$$g_{sw,x} = 0.001D_{s,x}, \quad (\text{Eq. S8})$$

where again  $x$  denotes abaxial or adaxial,  $g_{sw}$  has units of  $\text{mol m}^{-2} \text{s}^{-1}$ , and  $D_s$  has units of  $\text{stomata mm}^{-2}$ . We calculated boundary layer conductance for each surface from trichome density,  $D_t$ , as

$$g_{bw,x} = \left[ r_{bw,\min} + (r_{bw,\max} - r_{bw,\min}) \cdot \frac{H_x}{H_x + 1} \right]^{-1}, \quad (\text{Eq. S9})$$

where  $r_{bw,\min}$  and  $r_{bw,\max}$  ( $\text{m}^2 \text{s mol}^{-1}$ ) are values of boundary layer resistance in the absence of trichomes or in the limit of infinite trichome density, respectively, and  $H_x$  (unitless) is the relative trichome density for surface  $x$ .

Potential electron transport rate was calculated as

$$J = \frac{0.5}{\theta_j} \left( J_m + \phi i - \sqrt{(J_m + \phi i)^2 - 4\theta_j J_m \phi i} \right), \quad (\text{Eq. S10})$$

where  $J_m$  is maximum potential electron transport rate ( $\mu\text{mol m}^{-2} \text{s}^{-1}$ ),  $\phi$  is the effective maximum quantum yield of electrons from absorbed photosynthetic photon flux (PPFD),  $i$  is absorbed PPFD ( $\mu\text{mol m}^{-2} \text{s}^{-1}$ ), and  $\theta_j$  is a dimensionless curvature parameter.  $i$  was calculated as  $(1 - \rho)i_o$ , where  $i_o$  is the incident PPFD and  $\rho$  is leaf reflectance (unitless), estimated from trichome density as

$$\rho = \left[ \rho_{\min} + (\rho_{\max} - \rho_{\min}) \cdot \frac{H}{H + 1} \right]^{-1}, \quad (\text{Eq. S11})$$

where  $\rho_{\min}$  and  $\rho_{\max}$  are the values of reflectance with no trichomes and in the limit of infinite trichome density, respectively, and  $H$  is the relative whole-leaf trichome density. Estimation of  $V_m$ ,  $R_d$ ,  $\Gamma^*$ ,  $K_c$ ,  $K_o$ ,  $J_m$ ,  $\phi$ , and  $\theta_j$  are described in section B, Parameter estimation below.

Transpiration rate was calculated as

$$E = g_{tw}(\Delta w_a + s\delta), \quad (\text{Eq. S12})$$

where  $\Delta w_a$  ( $\text{mol mol}^{-1}$ ) is the vapor pressure deficit of the air expressed as a mole fraction, calculated as  $\Delta w_a = w_{sa} - w_a$ , where  $w_{sa}$  is the saturation water vapor mole fraction calculated at air temperature  $T_{ac}$  in  $^{\circ}\text{C}$  as  $w_{sa} = 0.006112 \cdot \exp[17.62T_{ac}/(243.12 + T_{ac})]$ , and  $w_a$  is the ambient water vapor mole fraction;  $s$  ( $\text{mol mol}^{-1} \text{K}^{-1}$ ) is the slope of saturation water vapor mole fraction vs temperature calculated as  $s = w_{sa}17.62 \times 243.12/(243.12 + T_{ac})^2$ ; and  $\delta$  (K) is the difference between leaf and air temperature;  $g_{tw}$  is total leaf conductance to water vapor, calculated as the sum of abaxial and adaxial values, which are given by

$$g_{tw,x} = (g_{sw,x}^{-1} + g_{bw,x}^{-1})^{-1}, \quad (\text{Eq. S12})$$

where  $x = \text{adaxial or abaxial}$ .  $\delta$  is calculated from the energy balance using an approximation that arises from linearizing the saturation vapor pressure response to temperature near leaf temperature, and omitting terms in  $\delta^2$ ,  $\delta^3$  and  $\delta^4$  from the expansion of  $T_{LK}^4$  as  $(T_{aK} + \delta)^4$  (where  $T_{aK}$  and  $T_{LK}$  are air and leaf temperatures, respectively, in K), giving

$$\delta = \frac{Q + (\epsilon_{\text{air}} - \epsilon_{\text{leaf}})\sigma T_{aK}^4 - \lambda g_{tw}\Delta w_a}{4\epsilon_{\text{leaf}}\sigma T_{aK}^3 + c_{pa}g_{bh} + \lambda g_{tw}s}, \quad (\text{Eq. S13})$$

where  $Q$  is absorbed shortwave radiation ( $\text{J m}^{-2} \text{s}^{-1}$ ),  $\sigma$  is the Stefan-Boltzmann constant ( $5.67 \times 10^{-8} \text{J m}^{-2} \text{s}^{-1} \text{K}^{-4}$ ),  $\epsilon_{\text{air}}$  is the IR emissivity of the atmosphere [ $0.642(w_a101325/T_{aK})^{1/7}$ ]; unitless),  $\epsilon_{\text{leaf}}$  is the leaf IR emissivity (0.98),  $\lambda$  is the latent heat of vaporization ( $4.4 \times 10^4 \text{J mol}^{-1}$ ),  $c_{pa}$  is the heat capacity of air ( $29.2 \text{J mol}^{-1} \text{K}^{-1}$ ), and  $g_{bh}$  is boundary layer conductance to heat, calculated as the sum of abaxial and adaxial values, given by

$$g_{bh,x} = \frac{g_{bw,x}}{1.08}, \quad (\text{Eq. S14})$$

where 1.08 is the ratio of the diffusion coefficients for water vapor and heat. We calculated  $Q$  as  $Q = 0.322i$ , where 0.322 converts from photosynthetic photon flux to total shortwave energy flux

based on the energy distribution of the shortwave spectrum (incident shortwave energy =  $0.5666i_0$ ; de Pury and Farquhar 1997) and the ratio of absorptances for total shortwave and visible radiation (0.568) given by Ehleringer and Mooney (1978).

## B. Parameter estimation

Marginal carbon cost of transpiration ( $\chi_w$ ). We estimated  $\chi_w$  by assuming, based on the equimarginal theorem, that when carbon investments in plant structure and function are optimized, the marginal carbon cost and revenue of transpiration are equal. The latter is  $(\partial A/\partial g_{sw})/(\partial E/\partial g_{sw})$ , for which a typical value under conditions of plentiful water supply would be on the order of  $400 \mu\text{mol CO}_2 \text{ mol}^{-1} \text{ H}_2\text{O}$ . We used that value for the “high moisture” environment, and values of 1000 and  $700 \mu\text{mol CO}_2 \text{ mol}^{-1} \text{ H}_2\text{O}$  to represent “low moisture” and “intermediate moisture” environments, respectively.

Marginal carbon cost of trichomes ( $\chi_t$ ). This parameter represents the direct carbon cost of construction for trichomes, not any indirect costs to growth, etc. We estimated  $\chi_t$  by arbitrarily assuming that the carbon content of trichomes represents 10% of the carbon content of the leaf when trichome density equals the population median in this study ( $165.5 \text{ mm}^{-2}$ ), then calculating leaf carbon content for a typical leaf with dry mass per area  $250 \text{ g m}^{-2}$  and 37% carbon by dry mass, and dividing by an effective amortization period of  $3.1 \times 10^6 \text{ s}$  (which scales midday, midsummer gas exchange rates to an effective annual total assuming sinusoidal diurnal and seasonal patterns (Buckley and Roberts, 2006)). These assumptions make amortized trichome C content commensurable with the instantaneous midday values of net photosynthesis calculated as described earlier. This calculation gives  $\chi_t = 0.25 \mu\text{mol m}^{-2} \text{ s}^{-1}$ , which also equals the amortized carbon cost of trichomes when  $H = 1$  (i.e., at median trichome density).

Boundary layer resistance with and without trichomes ( $r_{\text{bw,max}}$  and  $r_{\text{bw,min}}$ ). We calculated  $r_{\text{bw,min}}$  (the value in the absence of hairs) using expressions given by Nobel (1999), assuming a leaf characteristic dimension of 5 cm and wind speed of  $2 \text{ m s}^{-1}$ . These assumptions give  $r_{\text{bw,min}} = 0.613 \text{ m}^2 \text{ s mol}^{-1}$  at  $28^\circ\text{C}$ . We then assumed that trichomes of very high density would double the boundary layer resistance, based on Parkhurst (1976), giving  $r_{\text{bw,max}} = 1.226 \text{ m}^2 \text{ s mol}^{-1}$ .

Leaf albedo with and without trichomes ( $\rho_{\max}$ ,  $\rho_{\min}$ ). We estimated  $\rho_{\min}$  and  $\rho_{\max}$  from observations of Ehleringer and Mooney (1978) in *Encelia farinosa*, as  $\rho_{\min} = 0.19$  and  $\rho_{\max} = 0.71$ .

Environmental conditions. We assumed ambient CO<sub>2</sub> mole fraction,  $c_a$ , was 400  $\mu\text{mol mol}^{-1}$ ; ambient water vapor mole fraction was  $w_a = 0.02 \text{ mol mol}^{-1}$  (wet/mild environment), 0.015 (semi-arid environment) or 0.01 (dry/hot environment); incident PPFD was  $i_o = 1700 \mu\text{mol m}^{-2} \text{ s}^{-1}$ ; and air temperature was  $T_{ac} = 25^\circ\text{C}$  (wet/mild),  $35^\circ\text{C}$  (semi-arid) or  $40^\circ\text{C}$  (hot/dry).

Photosynthetic parameters. We arbitrarily set the value of  $V_m$  at  $25^\circ\text{C}$  as  $50 \mu\text{mol m}^{-2} \text{ s}^{-1}$  and assumed the values of  $J_m$  and  $R_d$  at  $25^\circ\text{C}$  were 2.1 and 0.01 times that of  $V_m$ , respectively (Wullschleger, 1993; de Pury and Farqhar, 1997). We calculated  $V_m$ ,  $J_m$  and  $R_d$  at the actual leaf temperature, and values of  $\Gamma^*$ ,  $K_c$ ,  $K_o$ ,  $\phi$  and  $\theta_j$  from temperature response functions given by Bernacchi et al. (2002, 2003).

### **C. Procedures used to generate four species sets**

We applied the model to each leaf in three “species sets”, simulated using the marginal density distributions for each variable (abaxial and abaxial  $D_s$  and  $D_t$ ) but modified and/or filtered to represent four extreme scenarios: whole-leaf  $D_s$  and  $D_t$  are completely uncorrelated (“independent” species set), perfectly negatively correlated due to a developmental trade-off (“trade-off”), or perfectly positively correlated due to a positive developmental constraint (“positive coordination”). We generated these three species sets as follows. First, we fitted density distribution functions to each variable in (abaxial and abaxial  $D_s$  and  $D_t$ ) in the California species data set. Then we sampled 1000 times from these marginal distributions to create a species set in which the four variables varied independently from one another. We repeated this procedure 1000 times using different randomization seeds, in each case eliminating species for which  $D_s$  or  $D_t$  for either surface was negative or whole-leaf  $D_s$  or  $D_t$  exceeded the maxima observed in the original species set, and selected the resulting species set that gave the weakest correlation between whole-leaf  $D_s$  and  $D_t$  ( $r = 0.000075$ ). This procedure left a species set of 842 species in which  $D_s$  and  $D_t$  were, for practical purposes, perfectly uncorrelated, which we refer to as the “independent” species set. We then generated three species sets by modifying the

independent species set. For the “positive coordination” species set, we replaced sampled values of whole-leaf  $D_t$  in the independent species set with values calculated from sampled whole-leaf  $D_s$  using the positive correlation in the original data set ( $D_t = 0.321D_s + 5.36$ ); This positive correlation represents the extreme scenario in which  $D_t$  and  $D_s$  are fully mutually determined by a positive developmental constraint. For the “trade-off” species set, we recalculated  $D_t$  as for the positive coordination case, but with the direction of the correlation reversed to simulate what would occur if  $D_t$  and  $D_s$  were fully mutually constrained by a developmental tradeoff, which gives  $D_t = 0.321[\max(D_s) - D_s] + 5.36$ , where the quantity  $\max(D_s) - D_s$  can be understood as a reflection (“flipping” horizontally) of the  $D_s$  axis.

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